

Date
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MTC-2

Unit-II

Laplace's correction of Newton's formula.
The Laplace formula is $v = \sqrt{\frac{\gamma P}{\rho}}$

[Error in Newton's formula for velocity of sound in air at ~~normal~~ N.T.P. \rightarrow

Normal air pressure = 76 cm
and Hg (Mercury) = $76 \times 13.59 \times 980$
dynes/cm² (p)

At 0°C and at normal atmospheric pressure, the density of ~~air = 0.001293 g/cm³~~
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So, from Newton's formula,

$$v = \sqrt{\frac{76 \times 13.59 \times 980}{0.001293}} \text{ (approx)}$$

This value of velocity of sound is ~~differs~~ 281 m/s
the ~~the~~ Laplace's correction of Newton's formula is \rightarrow :

This difference between the experimentally observed value of velocity of sound in air and the calculated value was explained by Laplace. He pointed out that during propagation of sound wave each layer of the medium is alternately compressed and rarefied.

During compression the layer is heated and during rarefaction the layer is cooled. On account of the fact that air is a bad conductor of heat as well as a bad radiator therefore heat cannot flow quickly from of ~~the~~ heated layers to the ~~the~~ cooled layers.

That is, the propagation of sound waves takes place under an adiabatic condition.

$$P \cdot V^\gamma = \text{constant}$$

where γ is the ratio of specific heat at constant pressure to the specific heat at constant volume.

Using the above relation Laplace showed that

$$V = \sqrt{\frac{\gamma P}{\rho}}$$

for air $\gamma = 1.41$,

Putting the value of γ we get

$V = 332 \text{ m/s}$ This result was given with the experimental value.